## 6.5630 Advanced Topics in Cryptography Problem Set 3 Optional PSET, No Due Date

This problem set has a single problem.

**Breaking Functional Encryption.** Recall the construction of a predicate encryption scheme supporting the *orthogonality predicate* (alternatively, linear functions with equality test) from the LWE assumption (see Lecture 8 notes, section 3). Such a function is defined by a vector  $y \in \mathbb{Z}_q^L$ , takes as input  $x \in \mathbb{Z}_q^L$  and outputs 1 if

$$\langle y, x \rangle = 0 \mod q$$

We showed in class that this construction is secure as a weakly hiding predicate encryption. That is, an adversary who gets secret keys corresponding to a number of vectors (linear functions)  $y_1, ..., y_k$  for a polynomially large k such that

$$\langle x, y_i \rangle \neq 0 \mod q$$
 for all  $i$ ,

cannot learn anything about x. Your task is to break this scheme when playing the strong hiding game. That is, when the challenge is (x, x') such that  $\langle x, y_i \rangle = \langle x', y_i \rangle \mod q$  for all *i* (but some of the inner products could be 0).

Concretely, you task is to design queries  $y_i$  such that the outputs  $\langle x, y_i \rangle \mod q$  does not reveal x, yet a ciphertext Enc(mpk, x) together with the secret keys  $sk_{y_1}, ..., sk_{y_\ell}$  completely reveals x.